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Effects of burst-and-coast
duty cycle on collective
behavior in a fish school
model

12th of January,
2026

**Collective behavior
2025/2026**



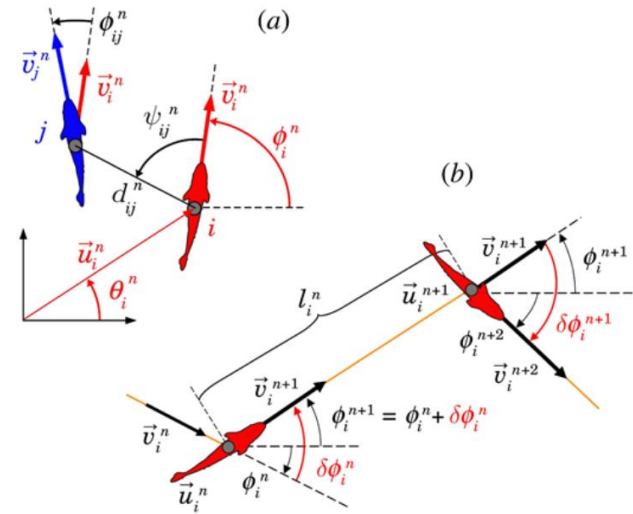
Problem

- Problem: burst-and-coast swimming
- Goal:
 - Re-implement the original article
 - Extend with:
 - Duty cycle
 - Decision steps



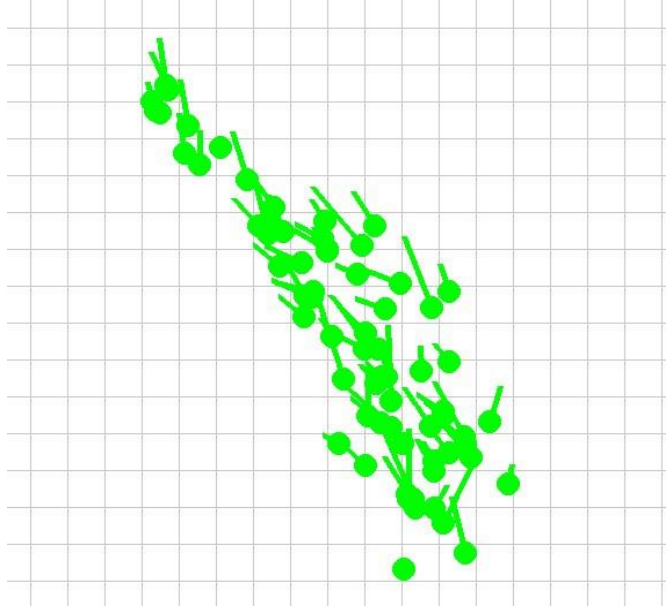
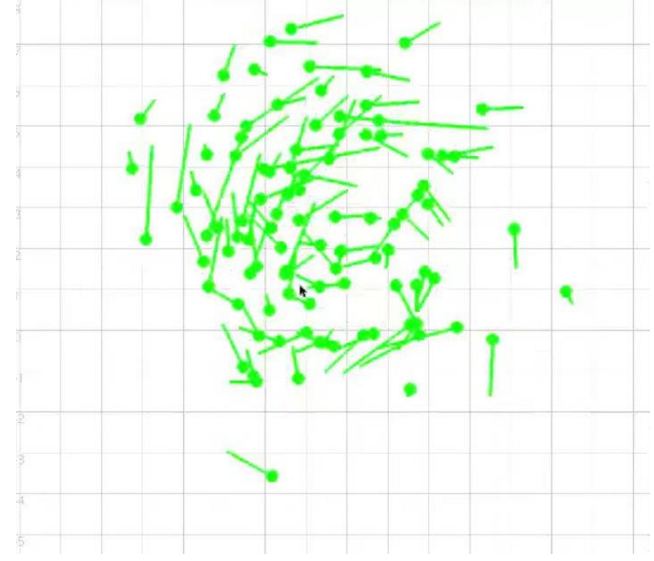
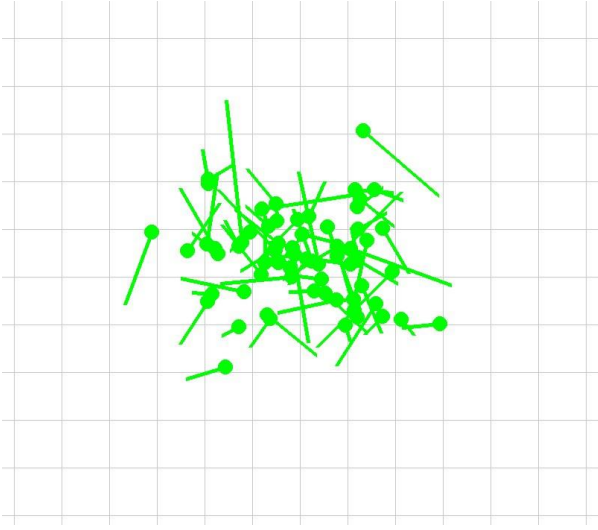
Baseline model

- Heading selection
- Burst phase (kick)
- Coast phase
- Repeat



Source: Wang et al.

- Python, numpy, pygame
- Discrete movement: instantaneous heading updates and position jumps





Extended model

- Implements continuous velocity integration
 - Duty cycle (ω):
 - Controls burst vs coast duration
 - Number of decision steps (n_ω)
 - Controls granularity of heading updates

$$\tau_{\text{burst}} = \omega \cdot \tau$$

$$\tau_{\text{coast}} = (1 - \omega) \cdot \tau$$



Evaluation

- Group dispersion:
 - how much the fish are spread out
- Group polarization
 - How aligned headings of fish are
- Milling index
 - how much the fish are swimming around a barycenter in a circular fashion

$$D(t) = \sqrt{\frac{1}{N} \sum_{i=1}^N \|\mathbf{u}_i(t) - \mathbf{u}_B(t)\|^2}$$

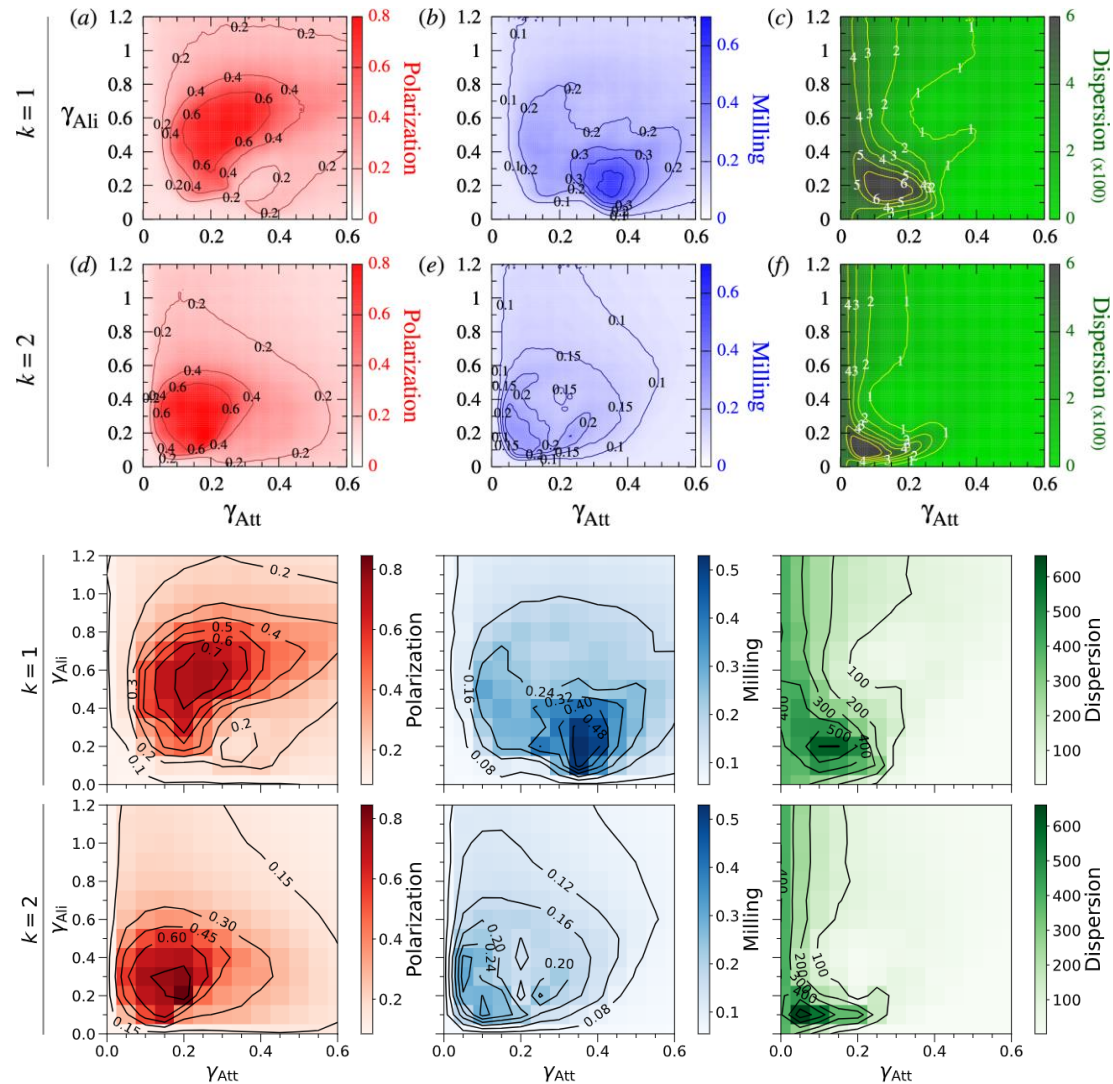
$$P(t) = \left\| \frac{1}{N} \sum_{i=1}^N \frac{v_i(t)}{\|v_i(t)\|} \right\|$$

$$M = \left| \frac{1}{N} \sum_{i=1}^N \sin(\bar{\theta}_w^i(t)) \right|$$



Results (base model)

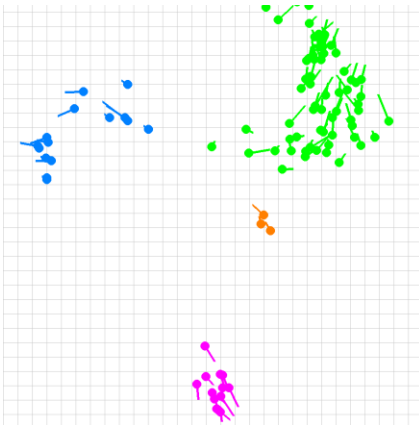
- Original vs base



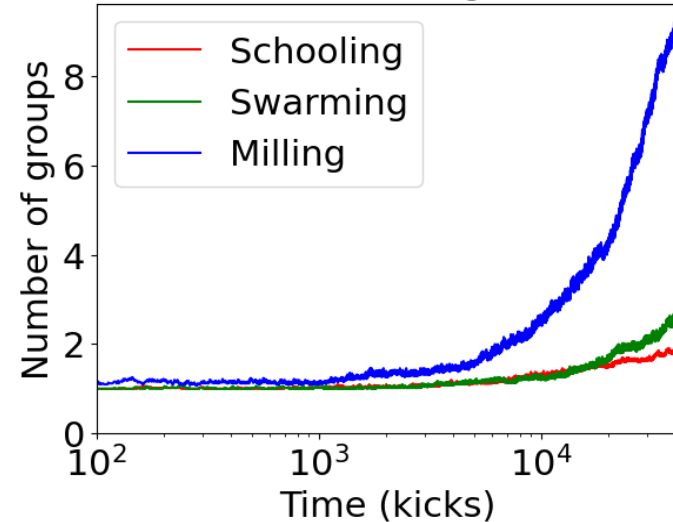


Results: number of groups

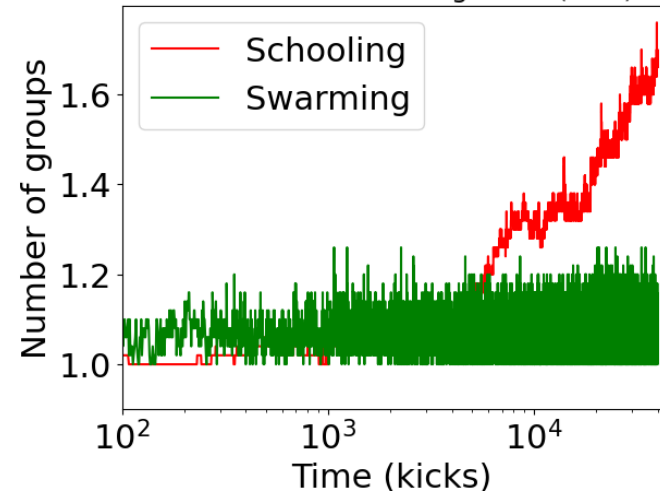
- Track number of groups over time
- Start with sequence of fish, separated by less than critical distance
- Merge groups that have at least one pair of fish, separated by less than merging distance



Number of groups through time for three different emergences ($k=1$)



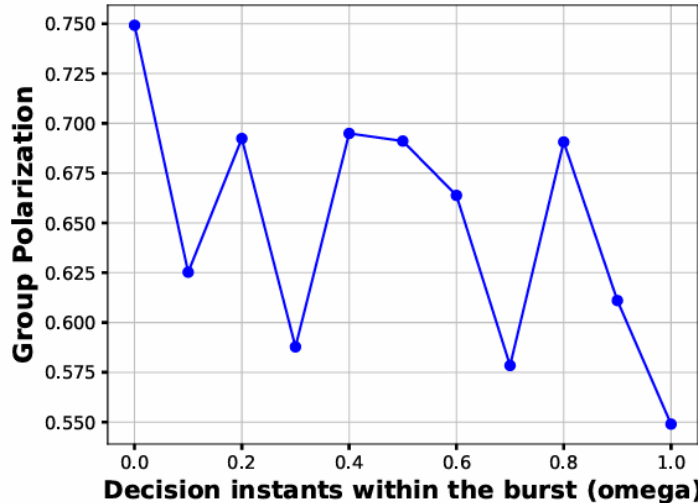
Number of groups through time for two different emergences ($k=2$)





Impact of ω

Effect of Decision Resolution on School Polarization

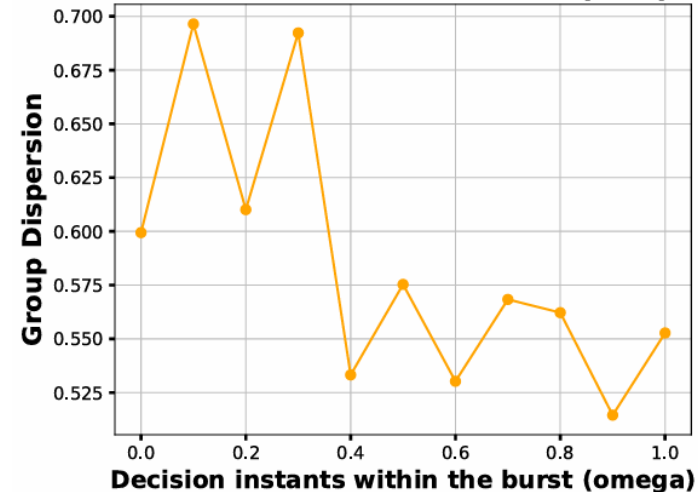


Effect of Decision Resolution on Milling Behavior



- Low ω :
 - short bursts, long coasts
 - High dispersion, fewer alignment opportunities, cheaper mistakes
- Intermediate ω :
 - High polarization, stable cohesion
- High ω :
 - Velocity magnitude stays high
 - Overshooting, continuous turning -> decreased polarization

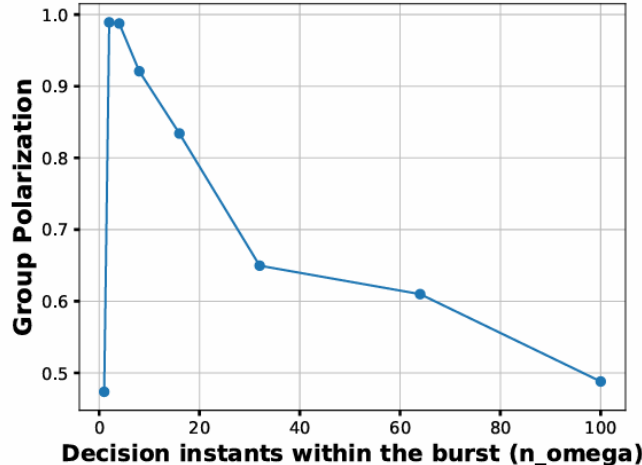
Effect of Decision Resolution on Group Dispersion



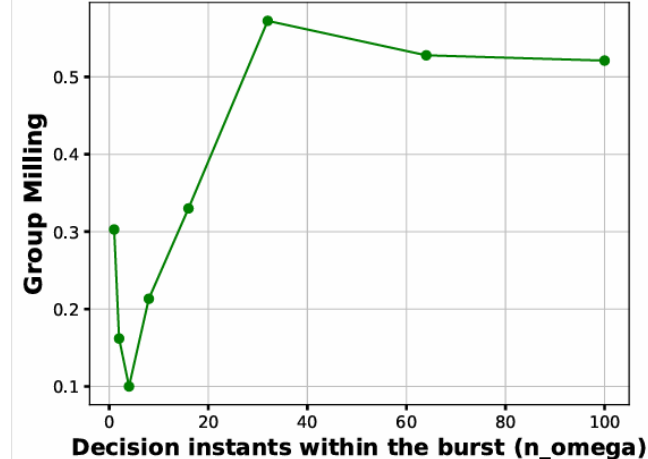


Impact of N_ω

Effect of Decision Resolution on School Polarization



Effect of Decision Resolution on Milling Behavior



Effect of Decision Resolution on Group Dispersion

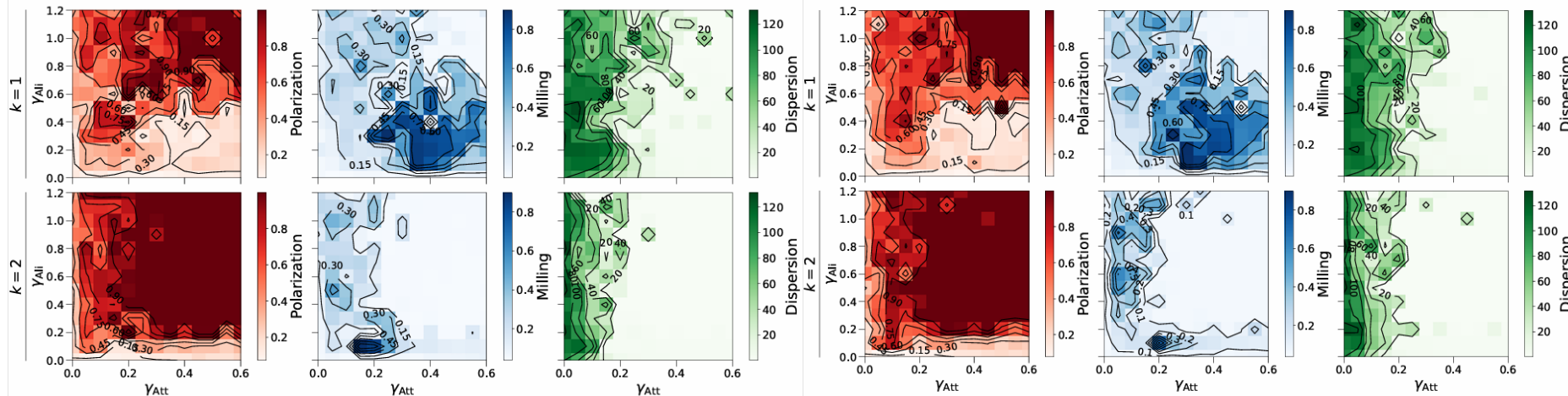
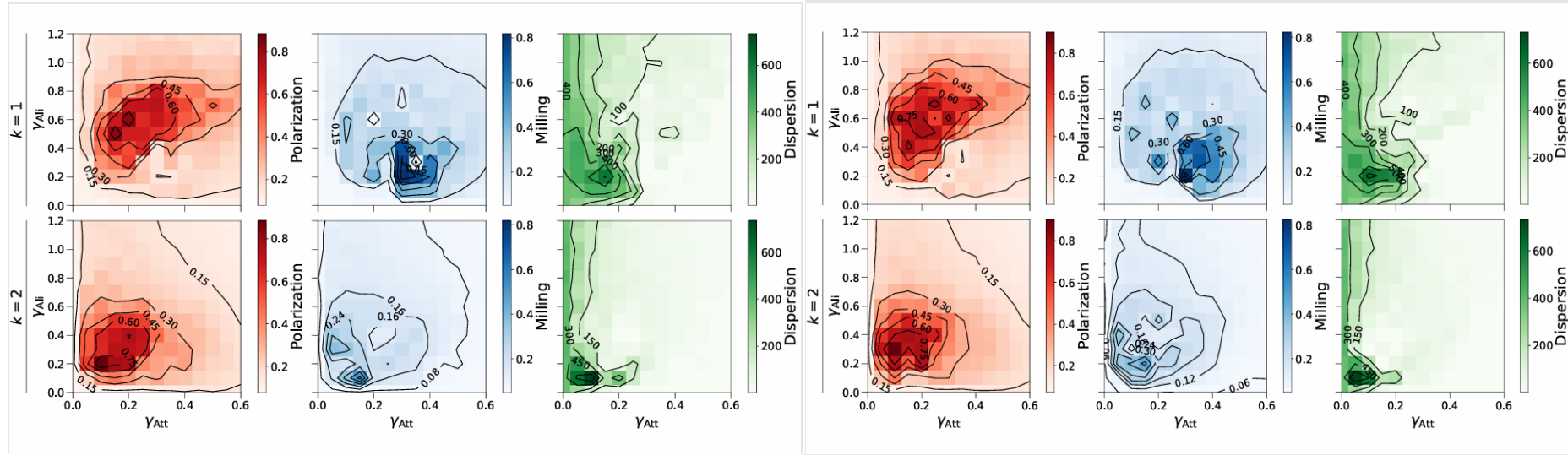


- $N_\omega = 1$ (single decision)
 - High instability -> fragmentation
- $N_\omega = 2-16$
 - Control is frequent enough to stabilize but not too frequent
- $N_\omega > 16$
 - Too frequent updates -> milling replaces polarization

Results (extended model)

$$\omega = 0, n_{\omega} = 1$$

$$\omega = 0.5, n_{\omega} = 1$$



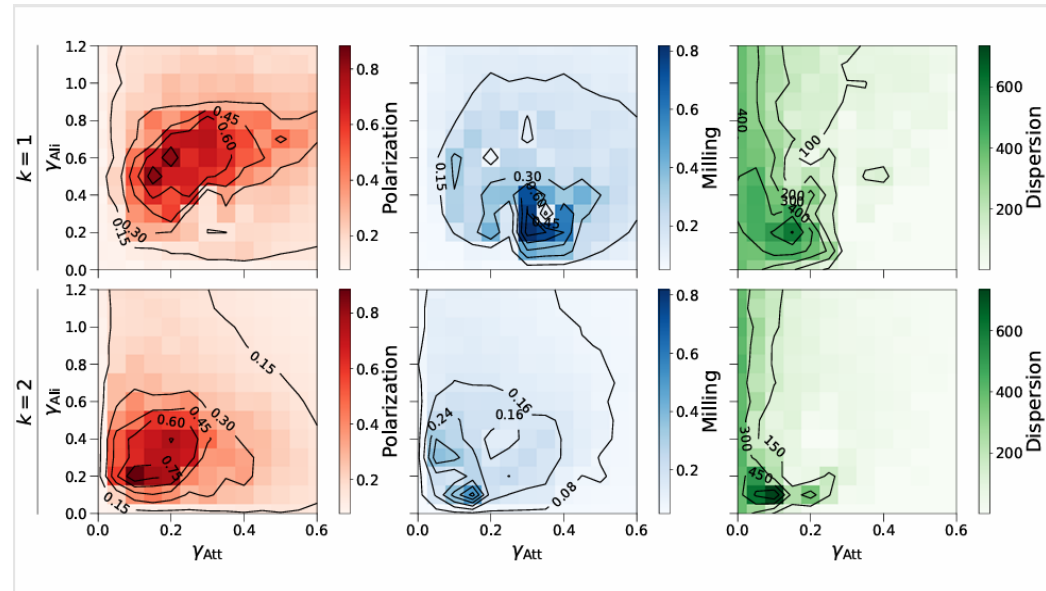
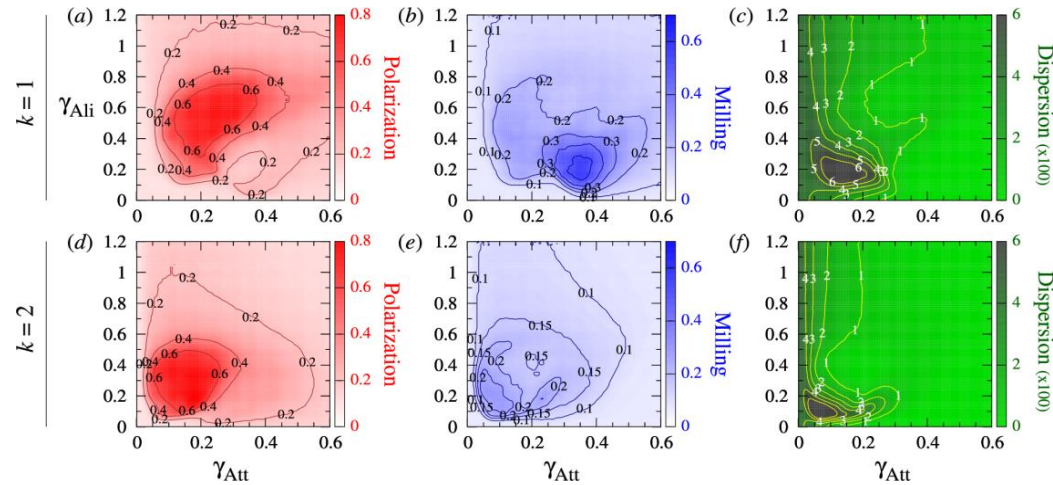
$$\omega = 0, n_{\omega} = 10$$

$$\omega = 0.5, n_{\omega} = 10$$



Extended results

- Base vs extended
- Confirmed with base model
- Increasing duty cycle improves cohesion but weakens precise alignment because inertia amplifies small heading differences
- Polarization peaks at intermediate decision resolution because too little control causes fragmentation, while too much control allows rotational modes to emerge and compete with alignment.



$$\omega = 0, n_{\omega} = 1$$



Conclusion & discussion

- Successfully re-implemented and extended a burst-and-coast model
- Key findings:
 - Intermediate duty cycles favor stable schooling
 - Intra-burst decisions are critical; a single decision might be insufficient for cohesion
- Biggest challenges:
 - Confirming if our results are correct
 - Lots of compute power needed
- Future work:
 - More realistic implementation:
 - Heterogeneity in speed, reaction time, noise
 - Global decision making, environmental interactions
 - More runs, bigger parameter sweep, larger simulations,... (just more compute power & time)